## TriadMathInc

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## Tiers 1-4: Syllabus

## Tier 1

## Tier 1 TI-30XA Calculator

TI-30XA Introduction
C1 ON/OFF FIX DEG M1 M2 M3
C2 Real Numbers: Add + Subtract - Equal =
C3 Negative Numbers $+\approx-$
C4 Multiply $\times$ Divide $\div$
C5 Percentage \%
C6 Memory M1, M2, M3 STO RCL ( )
C7 $\quad X^{2}$ Square
C8 $\sqrt{ } \mathrm{X}$ Square Root
C9 1/X Reciprocal "Flip It"
C10 Fractions $A^{B / C}+-\times \div$
C11 D/C Proper/Improper Fractions
C12 $\mathrm{F} \leftrightarrow \mathrm{D}$ Fraction to Decimal Conversion
C13 DEG RAD GRAD Three Angle Measures
C14 SIN SIN ${ }^{-1}$
C15 COS COS ${ }^{-1}$
C 16 TAN TAN ${ }^{-1}$

## Tier 1 Pre-Algebra

Pre-Algebra Introduction
P1 Real Numbers, Integers, and Rationals
P2 The Number Line, Negative Numbers
P3 Rules of Addition + -

P4 Rules of Multiplication $\times \div$
P5 Distributive Law + and $\times$ Combined
P6 Fractions, A/B and C/D, Rules
P7 Squares $X^{2} X$ Squared
P8 Square Roots $\sqrt{ } X$
P9 Reciprocal $1 / X \quad X \neq 0$
P10 Exponents $Y^{X} Y>0$, $X$ Can Be Any Number

## Tier 2

## Tier 2 Algebra

Introduction to Algebra
A1 Four Ways to Solve an Algebra Equation
A2 The Rule of Algebra
A3 $\quad X+A=B$ This is an Easy Linear Equation
A4 $\quad A X=B$ This is an Easy Linear Equation
A5 $\quad A X+B=C X+D$ This is an Easy Linear Equation
A6 $A / X=C / D$ This is an Easy Linear Equation
A7 $\quad A X^{2}=B$ This is an Easy Non-Linear Equation
A8 $\quad \mathrm{A} \sqrt{ } \mathrm{X}=\mathrm{B}$ This is an Easy Non-Linear Equation
A9 (1) SIN $X^{\circ}=A,-1 \leq A \leq 1$, or (2) $\operatorname{SIN}^{-1} X=A^{\circ}, 0 \leq A^{\circ} \leq 180^{\circ}$
A10 (1) $\operatorname{COS} X^{\circ}=A,-1 \leq A \leq 1$, or (2) $\cos ^{-1} X=A^{\circ}, 0 \leq A^{\circ} \leq 180^{\circ}$

## Tier 2 Geometry

Introduction to Geometry
G1 What is Geometry?
G2 Straight Lines and Angles
G3 Parallel Lines
G4 Triangles, Definition, Sum of Angles
G5 Pythagorean Theorem
G6 Similar Triangles
G7 Quadrilaterals, Polygons, Perimeters (P)
G8 Area of Triangles and Rectangles
G9 Formulas for Polygons
G10 Circles $\pi$ Circumference
G11 Circles Area $A=\pi r^{2}$
G12 Circles Special Properties
G13 Surface Area Blocks and Cylinders
G14 Surface Area Cones
G15 Volume Blocks and Cylinders
G16 Volume Cones
G17 Surface Area Ball or Sphere

G18 Volume Ball or Sphere, Archimedes Tombstone
G19 When Geometry is not Enough for Triangles

## Tier 2 Trigonometry

Introduction to Trigonometry
T1 Trig Functions SIN COS TAN
T2 SIN $X$, Sine of $X, X$ is an Angle (Degrees ${ }^{\circ}$ )
T3 $\operatorname{COS} X$, Cosine of $X, X$ is an Angle (Degrees ${ }^{\circ}$ )
T4 TAN $X$, Tangent of $X, X$ is an Angle (Degrees ${ }^{\circ}$ )
T5 Warning about SIN ${ }^{-1}$
T6 Law of Sines
T7 Law of Cosines - Generalized Pythagorean Theorem
T8 Trigonometry Beyond Practical Math (Optional)

## Tier 3

## Tier 3 Part 1

T3 Part 1 Introduction
T3 P1 L1 The Real Number System (Simmons pp. 34-36)
T3 P1 L2A Notation and Rules (Simmons pp. 36 -39)
T3 P1 L2B Notation and Rules (Simmons pp. 36 -39)
T3 P1 L3 Integral Exponents (Simmons pp. 39 -40)
T3 P1 L4 Root, Radical, Fractional Exponents (Simmons pp. 40-43)
T3 P1 L5 Polynomials (Simmons pp. 43-45)
T3 P1 L6 Factoring Polynomials (Simmons pp. 45 -46)
T3 P1 L7 Linear Equations \& Rule of Algebra (Simmons pp. 46 -49)
Plus: Review of Algebra and Rules from the Tier 2 Practical Math Foundation
T3 P1 L8 Quadratic Equation (Simmons pp. 46 -49)
T3 P1 L9 Inequalities and Absolute Values (Simmons pp. 49-50)
T3 P1 L10 Coordinates in a Plane (Simmons pp. $53-54$ )
T3 P1 L11 Functions and Graphs (Simmons pp. 51 -53)
T3 P1 L12 Straight Lines \& Linear Functions (Simmons pp. 55-56)
T3 P1 L13 Parallel and Perpendicular Lines (Simmons pp. 55-56)
T3 P1 L14 Intersecting Straight Lines (Custom Training) You will learn a process you should master by practice.

Part 1 of Tier 3 should prepare you for a standard test you will need to pass to graduate from high school.

Part 2 of Tier 3 will teach you additional mathematics you will need to excel on the SAT and ACT and other exams.

## Tier 3 Part 2

T3 P2 L1 Prime Numbers (Custom Notes)
T3 P2 L2 Number Facts and Ideas (Custom Notes)
T3 P2 L3 Percents and Percentage (Custom Notes)
T3 P2 L4 Chain Discounts (Custom Notes)
T3 P2 L5 Markups and Discounts (Custom Notes)
T3 P2 L6 Means, Medians, Averages (Custom Notes)
T3 P2 L7 Ratios and Proportions (Custom Notes)
T3 P2 L8 Logic (Custom Notes)
T3 P2 L9 Arithmetic Progressions (Simmons pp. 77)
T3 P2 L10 Geometric Progressions (Simmons pp. 74-76)
T3 P2 L11 Geometric Series (Simmons pp. 74-76)
T3 P2 L12 Permutations and Combinations (Simmons pp. 78-81)
T3 P2 L13 Combinations (continued) (Simmons pp. 78-81)
T3 P2 L14 Probability (Custom Notes)

## Tier 3 Part 3: SAT/ACT Preparation

T3 P2 L1 Pep Talk
T3 P2 L2 Test Preparation
T3 P2 L3 Test Techniques
T3 P2 L4 Sample Problems A
T3 P2 L5 Sample Problems B
T3 P2 L6 Sample Problems C
T3 P2 L7 Sample Problems D
T3 P2 L8 More Fun
T3 P2 L9 Fun \& Games

## Tier 4

Precalculus Mathematics in a Nutshell, and Notes will be used. Geometry, Algebra, Trigonometry, and Complex Numbers, with Wolfram-Alpha will be covered.

T4I Introduction to Tier 4, and Overview
Tier 4 Geometry
G1 Introduction to Geometry Overview (pp. 2-3)
G2 Triangles: Angles, Parallel Lines, Area (pp. 4-5)
G3 Triangles: Similar Congruent (p. 6)
G4 Pythagorean Theorem (pp. 6-7)
G5 Circles: Pi, Area, Sector (pp. 7-8)
G6 Circles: Inscribed angles (pp. 8-9)

G7 Circles: Tangents \& Constructions (Notes)
G8 Angles: Bisect, Trisect, Compass, Impossibilities (Notes)
G9 Cylinder: Area, Volume (pp. 9-10)
G10 Cone: Overview (pp. 10-11)
G11 Cone: Problems - Help (pp. 21-22)
G12 Cone: Optional Proof for Math Majors (Simmons)
G13 Sphere: Volume and Area, Problems (pp. 22-23)
G14 Sphere: Optional Proof with Cavalieri's Principle (pp. 13-14)

## Interlude \#1

## Tier 4 Algebra

A1 Introduction to Algebra, Rules of Algebra Review (p. 33)
A2 Basics: Numbers (pp. 34-35)
A3 Review - Overview Tier 3 (pp. 36-50)
A4 Review - Overview Tier 3 (pp. 51-56)
*A5 Introduction to Wolfram-Alpha (Notes)
A6 Circles (pp. 57-58)
A7 Ellipses (Notes)
A8 Parabolas (pp. 58-60)
A9 Hyperbolas (Notes)
A10 Conic Sections
A11 Functions and Graphs (pp. 60-62)
A12 Polynomial Division (pp. 65-67)
A13 Logarithms Calculator (pp. 63-65)
A14 Logarithms Exponents (Notes)
A15 Examples Log Scale

## Interlude \#2

## Tier 4 Trigonometry

T1 Introduction to Trigonometry (pp. 92-93)
T2 Review of some Analytical Geometry (pp. 93-96)
T3 Radian Measure (pp. 96-98)
T4 Trig Functions Circle Definition (pp. 98-100)
T5 Trig Identities Intro (pp. 100-101)
T6 Evaluating Trig Functions (pp. 101-103)
T7 Trig functions graphs (pp. 103-105)
T8 Frequency and Phase (Notes)
T9 Identities pp 105-6 sec 4 (pp. 114-5)
T10 Identities and Graphs (Notes)
T11 Proofs of Identities - Appendix B (pp. 111-112)

T12 Inverse Trig Functions (pp. 107-109)
T13 Law of Sines and Cosines (p. 109)

## Tier 4 Complex Numbers

Complex Numbers will be treated with a modern geometric approach. Real Numbers correspond to points on a straight line Complex Numbers correspond to points in the plane. Complex Numbers have many wonderful geometric properties that relate geometry and algebra. Trigonometry is more fully understood when one understands complex numbers. Euler's identity is the key to this. Complex numbers are very powerful and indispensable in modern STEM subjects.

C1 Real Numbers Synopsis
C2 Complex Number Definition
C3 Complex Numbers Geometry
C4 Complex Number Geometry Proof
C5 Interlude for Inspiration $y^{\wedge} x$
C6 Interlude Preparation
C7 Wonderful Equation
C8 Motivation for Wonderful Equation
C9 Roots of Unity
C10 Clocks and Frequency
C11 Exponents and Logarithms
Tier 4 Algebra Special Topics
AST1 Mathematical Induction (pp. 83-84)
AST2 Progressions, Permutations, Combinations Review Tier3 (pp. 74-80)
AST3 Binomial Theorem (pp. 81-82)
AST4 Linear Equations Determinants (pp. 68-70)
AST5 Linear Equations 3D (pp. 71-73)
AST6 Cone and Sphere, Calculus Preview (pp. 84-87)
Tier 4 Geometry Special Topics for Math Majors/Teachers
GST1 Review of Geometry
GST2 Ceva's Theorem (pp. 27-29)
GST3 Heron's \& Brahmagupta's Formulae (p. 18, Problem 20, pp. 30-31)
GST4 Geometry and Algebra, Analytical Geometry
GST5 Euclid Geometry vs Non-Euclidean Geometries
GST6 Calculus Preview

